

# On D-brane anti D-brane effective actions and their corrections to all orders in alpha-prime

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## Abstract

Based on a four point function, the S-matrix elements at disk level of the scattering amplitude of one closed string Ramond-Ramond field ( $C$ ) and two tachyons and one scalar field, we find out new couplings in brane anti brane effective actions for  $p = n, p + 2 = n$  cases. Using the infinite corrections of the vertex of one RR, one gauge and one scalar field and applying the correct expansion, it is investigated in details how we produce the infinite gauge poles of the amplitude for  $p = n$  case. By discovering new higher derivative corrections of two tachyon-two scalar couplings in brane anti brane systems to all orders in  $\alpha'$ , we also obtain the infinite scalar poles in  $t' + s' + u$ -channel in field theory. Working with the complete form of the amplitude with the closed form of the expansion and comparing all the infinite contact terms of this amplitude, we derive several new Wess-Zumino couplings with all their infinite higher derivative corrections in the world volume of brane anti brane systems. In particular, in producing all the infinite scalar poles of  $\langle V_C V_\phi V_T V_T \rangle$ , one has to consider the fact that scalar's vertex operator in  $(-1)$ -picture must carry the internal  $\sigma_3$  Chan-Paton matrix. The symmetric trace effective action has a non-zero coupling between  $D\phi^{(1)i}$  and  $D\phi_i^{(2)}$  while this coupling does not exist in ordinary trace effective action.

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# 1 Introduction

The relation between closed string Ramond-Ramond field and D-branes was widely realized in [1]. It is worthwhile to refer some main references on branes [2, 3, 4]. To review within full details Dirac-Born-Infeld and Wess-Zumino effective actions [5, 6, 7, 8, 9] and all references there might be considered.

In this paper we would like to deal with non-BPS branes and in particular we look for new couplings (which can be explored just by S-matrix calculations) in the world volume of brane anti brane systems in II super string theory, with spatial dimension of  $D_p$ -branes becomes odd (even) for IIA(IIB) string theory.

Studying tachyons in super string theories may provide some good information about these theories in some backgrounds which are time-dependent [10, 11, 12, 13, 14]. Based on some arguments [14], we highlight the point that the effective theory of all non-BPS branes does involve just massless states and tachyon. To be able to proceed with non-BPS branes in string theory and with their applications, one should take into account [11, 12, 15]. The complete form of the effective actions of non-BPS branes was introduced in [16, 17].

The only consistent effective action for D-brane anti D-brane systems, based on direct S-matrix computations of one closed string Ramond-Ramond, two tachyons and one gauge field was appeared in [18, 19]. In [19] we have shown that there was a non-zero coupling between  $F^{(1)}$  and  $F^{(2)}$  and we found all their infinite higher derivative corrections. Note that for ordinary trace prescription, this coupling does not exist. It is important to emphasize that the effective action in [20] is not consistent with S-matrix computations and in fact symmetrized trace works out for super string computations. In this paper we find new couplings between  $D\phi^{(1)i}$  and  $D\phi_i^{(2)}$ . Having set the tachyon to zero, both ordinary and symmetric trace effective actions become equivalent.

In order to observe the details on tachyon condensation for brane anti brane system [21] has been constructed, moreover some of the the Ramond-Ramond couplings on the world volume of brane anti brane have been discussed with in all needed details in [22, 19].

Although several motivations with their explanations have been explained in [17], it is important to emphasize some of them very briefly and refer to all references that appeared in [17].

The first motivation is actually related to dualities [23]. The second one somehow should be taken as a matter of brane production in which we are not going to go through details

so just to clarify more [24, 25] might be useful to look in. Indeed if the distance between brane anti brane is less than string's scale, then we will have two real tachyons in brane anti brane's spectrum. The third motivation is to have inflation in string theory, one might consider brane anti brane effective action [19] in which brane and anti brane have to be separated [26, 27, 28], in which this formalism was explained in detail in the section 2.1 of [17]. The fourth motivation for studying tachyons is indeed, working out with holographic models in QCD [29, 30]. The last motivation is that, S-Matrix computation does have strong potential to explore several new couplings with having no on-shell ambiguity.

Having set some arguments [31, 22], one can talk about the Wess-Zumino effective action for the tachyons by applying super connection approach [32].

Note that the super connection's curvature just for brane anti brane has been achieved in [19] and it is generalized in [17] to actually take several couplings between gauge, tachyon and Ramond-Ramond field in the branes' world volume directions.

However the couplings between scalar field, RR and tachyons can not be derived by making use of the multiplication rule of the super matrices. The only way to discover these new couplings on the longitudinal and transverse directions of the brane anti brane is just based on scattering amplitude techniques. In [5, 33] we found all the infinite corrections to BPS branes and in particular special attention was paid to a conjecture on higher derivative corrections for both BPS and non-BPS branes in [34] and the their applications to some dualities [35], Ads/CFT correspondence and in M-theory [36] were argued.

In the next section we would like to compute in detail the amplitude of one RR, two tachyons and one scalar field in the world volume of brane anti brane systems. Then we move on momentum expansion and discuss about a particular expansion. The goal of this paper is to derive with explicit computations the effective actions of brane anti brane systems and to discover several new couplings with all their infinite  $\alpha'$  corrections. In section 3.1 we find all infinite u-channel gauge poles with all infinite contact interactions for  $p = n$  case. We find some new couplings like  $\partial_i C_{p-1} \wedge DT \wedge DT^* (\phi^1 + \phi^2)^i$ , we also find its infinite higher derivative corrections and fix its coefficient by making use of the  $C\phi TT$  amplitude. Then we go on to achieve all infinite  $\alpha'$ -higher derivative corrections of two tachyon, two scalar couplings and in particular we show that these new corrections of brane anti brane system are completely different from non-BPS branes [17]. We check these new two tachyon, two scalar couplings of brane anti brane system by producing all infinite scalar pole in  $u + s' + t'$ - channel for  $p + 2 = n$  case. For  $p + 2 = n$  case we also obtain a new coupling like  $\epsilon^{a_0 \dots a_p} H_{ia_0 \dots a_p} (\phi^{(1)} - \phi^{(2)})^i TT^*$  and fix its coefficient as well.

Eventually we explore the presence of the new terms involving  $D\phi^{i(1)}.D\phi_i^{(2)}$  in DBI action of brane anti brane systems.

## 2 The four point amplitude between one RR, one scalar field and two tachyons ( $C\phi TT$ )

In order to find the infinite higher derivative corrections of between two tachyon, two scalar couplings in the world volume of brane anti brane systems with exact coefficients, we have to have the complete form of the amplitude of  $C\phi TT$ . One might wonder whether the new two scalar two tachyon couplings of non-BPS branes [17] could be applied to actually match infinite scalar poles of the amplitude of  $C\phi TT$  in the world volume of brane anti brane systems with its field theory side.

In this paper within details we will point out that two scalar two tachyon couplings of brane anti brane systems to all orders are completely different from two tachyon two scalar couplings of non-BPS branes [17] and indeed we observe in a clear way that making use of those non-BPS couplings we get inconsistent result and we are not able to match all infinite scalar poles of the string theory amplitude of  $C\phi TT$  with its field theory.

With this remarkable motivation we start discovering in detail the S-matrix elements of  $C\phi TT$ .

The four point amplitude between one closed string RR, one gauge field and two tachyons  $CATT$  in detail in [19] has been done. Setting all physical state conditions we observe that there are various subtleties in the mixed open-closed tree level amplitudes where we will point out some of them later on.

Nevertheless, let us make some concrete arguments based on field theory analysis. Therefore before getting to the computations, we want to make some comments about apparent similarities between  $CATT$  and  $C\phi TT$  amplitudes. The amplitude for  $C\phi TT$  for  $p = n$  case does include the infinite gauge poles and also for  $p + 2 = n$  case, this amplitude does involve the infinite scalar poles. Notice that due to some kinematic constraints  $C\phi TT$  does not have any tachyon pole while  $CATT$  in addition to infinite gauge poles has infinite tachyon poles for  $p = n$  case.

The other fact which comes out from the direct computation is that for  $C\phi TT$  amplitude neither in  $p = n$  nor in  $p + 2 = n$  case we do not have any double pole. This is important to highlight the fact that after long computations we found a double pole for  $p = n$  case in  $CATT$  amplitude. The other fact is that the S-matrix of  $C\phi TT$  will make sense for  $p = n, p + 2 = n$  cases while the amplitude of  $CATT$  was made of  $p - 2 = n, p = n$  cases.

The other motivation for performing the calculations of  $C\phi TT$  is that, we could discover several new Wess-Zumino couplings meanwhile they are completely absent in  $CATT$  amplitude[19]. Therefore by some well known CFT methods in the world volume of brane anti brane systems and in particular in type II super string theory, we start finding S-matrix of two tachyons, one scalar field and one closed string RR field to indeed derive new couplings with all their higher derivative corrections to all orders in  $\alpha'$ . Needless to say that the idea of obtaining closed form of higher derivative corrections to all orders is quite amazing.

This  $C\phi TT$  amplitude in brane anti brane system's world volume can be written down as follows

$$\mathcal{A}^{C\phi TT} \sim \int dx_1 dx_2 dx_3 dz d\bar{z} \langle V_\phi^{(0)}(x_1) V_T^{(0)}(x_2) V_T^{(0)}(x_3) V_{RR}^{(-\frac{3}{2}, -\frac{1}{2})}(z, \bar{z}) \rangle.$$

Note that we do have two more freedoms to find out the amplitude of  $C\phi TT$ , like working out either with

$$\langle V_\phi^{(-1)}(x_1) V_T^{(0)}(x_2) V_T^{(0)}(x_3) V_{RR}^{(-\frac{1}{2}, -\frac{1}{2})}(z, \bar{z}) \rangle$$

or

$$\langle V_\phi^{(0)}(x_1) V_T^{(-1)}(x_2) V_T^{(0)}(x_3) V_{RR}^{(-\frac{1}{2}, -\frac{1}{2})}(z, \bar{z}) \rangle$$

One remarkable fact about tachyon's vertex operator in string theory is that it does relate to two real components of the complex tachyon in field theory which means that the following relation holds

$$T = \frac{1}{\sqrt{2}}(T_1 + iT_2) \quad (1)$$

In order to avoid so much details we try to look for  $C\phi TT$  amplitude in the following picture

$$\mathcal{A}^{C\phi TT} \sim \int dx_1 dx_2 dx_3 dz d\bar{z} \langle V_\phi^{(-1)}(x_1) V_T^{(0)}(x_2) V_T^{(0)}(x_3) V_{RR}^{(-\frac{1}{2}, -\frac{1}{2})}(z, \bar{z}) \rangle, \quad (2)$$

Indeed it is the fastest way to carry out  $C\phi TT$  amplitude without making use of applying several physical state conditions and Bianchi identities. To clarify all things once more in

this paper we express the general form of vertices for our amplitude<sup>2</sup>

$$\begin{aligned}
V_T^{(0)}(x) &= \alpha' i k \cdot \psi(x) e^{\alpha' i k \cdot X(x)} \lambda \otimes \sigma_1 \\
V_\phi^{(-1)}(y) &= \xi_i e^{-\phi(y)} \psi^i(y) e^{\alpha' i q \cdot X(y)} \lambda \otimes \sigma_3 \\
V_{RR}^{(-1)}(z, \bar{z}) &= (P_- \mathbb{H}_{(n)} M_p)^{\alpha\beta} e^{-\phi(z)/2} S_\alpha(z) e^{i \frac{\alpha'}{2} p \cdot X(z)} e^{-\phi(\bar{z})/2} S_\beta(\bar{z}) e^{i \frac{\alpha'}{2} p \cdot D \cdot X(\bar{z})} \otimes \sigma_3
\end{aligned} \tag{3}$$

Note that due to non-zero couplings between two tachyons and one RR in brane anti brane systems [19, 22] the CP factor for RR for brane anti brane in (-1)-picture (which is  $\sigma_3$ ) is different from CP factor for RR in non-BPS branes which is  $\sigma_3 \sigma_1$ .

$k$  is tachyon's momentum which satisfies  $k^2 = \frac{1}{4}$  and physical state conditions for scalar is  $k_2 \cdot \xi = k_1 \cdot \xi = q \cdot \xi = 0$ . The scalar in (-1)-picture does accompany  $\sigma_3$  factor, the so called internal degree of freedom. Notice that the other CP factors of open strings and RR closed string for diverse pictures[17] is introduced. Thus our amplitude has  $\text{Tr}(\sigma_3 \sigma_3 \sigma_1 \sigma_1) = 2$  factor. The projector in closed string is  $P_- = \frac{1}{2}(1 - \gamma^{11})$  and

$$\mathbb{H}_{(n)} = \frac{a_n}{n!} H_{\mu_1 \dots \mu_n} \gamma^{\mu_1} \dots \gamma^{\mu_n} ,$$

with  $n = 2, 4, a_n = i$  ( $n = 1, 3, 5, a_n = 1$ ) for IIA (IIB). Having used doubling trick [17], we now replace fields to a total complex plane which means that the following change of variables have to be considered

$$\tilde{X}^\mu(\bar{z}) \rightarrow D_\nu^\mu X^\nu(\bar{z}) , \quad \tilde{\psi}^\mu(\bar{z}) \rightarrow D_\nu^\mu \psi^\nu(\bar{z}) , \quad \tilde{\phi}(\bar{z}) \rightarrow \phi(\bar{z}) , \quad \text{and} \quad \tilde{S}_\alpha(\bar{z}) \rightarrow M_\alpha^\beta S_\beta(\bar{z}) ,$$

with

$$D = \begin{pmatrix} -1_{9-p} & 0 \\ 0 & 1_{p+1} \end{pmatrix} , \quad \text{and} \quad M_p = \begin{cases} \frac{\pm i}{(p+1)!} \gamma^{i_1} \gamma^{i_2} \dots \gamma^{i_{p+1}} \epsilon_{i_1 \dots i_{p+1}} & \text{for } p \text{ even} \\ \frac{\pm 1}{(p+1)!} \gamma^{i_1} \gamma^{i_2} \dots \gamma^{i_{p+1}} \gamma_{11} \epsilon_{i_1 \dots i_{p+1}} & \text{for } p \text{ odd} \end{cases}$$

Once more, it is worth pointing out the needed correlators  $X^\mu, \psi^\nu, \phi$ , as below

$$\begin{aligned}
\langle X^\mu(z) X^\nu(w) \rangle &= -\frac{\alpha'}{2} \eta^{\mu\nu} \log(z - w) , \\
\langle \psi^\mu(z) \psi^\nu(w) \rangle &= -\frac{\alpha'}{2} \eta^{\mu\nu} (z - w)^{-1} , \\
\langle \phi(z) \phi(w) \rangle &= -\log(z - w) .
\end{aligned} \tag{4}$$

By applying  $x_4 \equiv z = x + iy$  and  $x_5 \equiv \bar{z} = x - iy$ , one can get the  $C\phi TT$  amplitude as

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<sup>2</sup>In string theory, one does set  $\alpha' = 2$ .

$$\begin{aligned} \mathcal{A}^{C\phi TT} &\sim 2 \int dx_1 dx_2 dx_3 dx_4 dx_5 (P_- \not{H}_{(n)} M_p)^{\alpha\beta} \xi_{1i} k_{2a} (-\alpha'^2 k_{3b}) x_{45}^{-1/4} (x_{14} x_{15})^{-1/2} I \\ &\times <: S_\alpha(x_4) : S_\beta(x_5) : \psi^i(x_1) : \psi^a(x_2) : \psi^b(x_3) > \text{Tr}(\lambda_1 \lambda_2 \lambda_3), \end{aligned} \quad (5)$$

where

$$I = |x_{12}|^{\alpha'^2 k_1 \cdot k_2} |x_{13}|^{\alpha'^2 k_1 \cdot k_3} |x_{14} x_{15}|^{\frac{\alpha'^2}{2} k_1 \cdot p} |x_{23}|^{\alpha'^2 k_2 \cdot k_3} |x_{24} x_{25}|^{\frac{\alpha'^2}{2} k_2 \cdot p} |x_{34} x_{35}|^{\frac{\alpha'^2}{2} k_3 \cdot p} |x_{45}|^{\frac{\alpha'^2}{4} p \cdot D \cdot p}$$

such that  $x_{ij} = x_i - x_j$  has been used. Applying the Wick-like rule [37] and [16, 5] to our case we end up with the correlation function involving three fermions ( $\psi$ s) and two spin operators as

$$\begin{aligned} <: S_\alpha(x_4) : S_\beta(x_5) : \psi^i(x_1) : \psi^a(x_2) : \psi^b(x_3) : > = \left[ (\Gamma^{bai} C^{-1})_{\alpha\beta} - 2\eta^{ab} \frac{Re[x_{24} x_{35}]}{x_{23} x_{45}} (\gamma^i C^{-1})_{\alpha\beta} \right] \\ \times 2^{-3/2} x_{45}^{1/4} (x_{14} x_{15} x_{24} x_{25} x_{34} x_{35})^{-1/2} \end{aligned} \quad (6)$$

Embedding (6) into our amplitude, we were able to check the  $SL(2, R)$  invariance of the S-matrix of  $C\phi TT$ . We wish to fix the location of the open strings in special places, that is

$$x_1 = 0, \quad x_2 = 1, \quad x_3 \rightarrow \infty,$$

By using this particular gauge fixing, we get to the following integrals

$$\int d^2 z |1 - z|^a |z|^b (z - \bar{z})^c (z + \bar{z})^d, \quad (7)$$

where  $d = 0, 1, 2$  and  $a, b, c$  should be given in terms of the Mandelstam variables as below

$$s = -\frac{\alpha'}{2} (k_1 + k_3)^2, \quad t = -\frac{\alpha'}{2} (k_1 + k_2)^2, \quad u = -\frac{\alpha'}{2} (k_2 + k_3)^2.$$

The result of the integrations for just  $d = 0, 1$  was expressed in [38], however if the computations were done in  $C^{-2} \phi^0 T^0 T^0$  picture we would need the result of the integrations for  $d = 2$  as well, which was performed in [17].

After some computations now we write down the complete form of  $C\phi TT$ ,

$$\mathcal{A}^{C\phi TT} = \mathcal{A}_1 + \mathcal{A}_2 \quad (8)$$

so that

$$\begin{aligned}
\mathcal{A}_1 &\sim -8\xi_{1i}k_{2a}k_{3b}2^{-3/2}\text{Tr}(P_- \not{H}_{(n)} M_p \Gamma^{bai}) L_1, \\
\mathcal{A}_2 &\sim -8\xi_{1i}2^{-3/2} \left\{ \text{Tr}(P_- \not{H}_{(n)} M_p \gamma^i) \right\} L_2
\end{aligned} \tag{9}$$

It should be emphasized that the closed form of  $\langle V_C V_\phi V_T V_T \rangle$  does not vanish only for  $p = n$  and  $p + 2 = n$  cases. As a matter of fact we observe that  $\mathcal{A}_1$  (first part of amplitude) in (9) is antisymmetric under interchanging two tachyons or under replacing  $2 \leftrightarrow 3$ . This does show that the first part of this four point function for  $p = n$  case should be vanished for both one RR and two real  $T_1$  tachyons and one RR and two  $T_2$ 's .

$L_1, L_2$  are made of

$$\begin{aligned}
L_1 &= (2)^{-2(t+s+u)-1} \pi \frac{\Gamma(-u)\Gamma(-s+\frac{1}{4})\Gamma(-t+\frac{1}{4})\Gamma(-t-s-u)}{\Gamma(-u-t+\frac{1}{4})\Gamma(-t-s+\frac{1}{2})\Gamma(-s-u+\frac{1}{4})}, \\
L_2 &= -(2)^{-2(t+s+u+1)} \pi \frac{\Gamma(-u+\frac{1}{2})\Gamma(-s+\frac{3}{4})\Gamma(-t+\frac{3}{4})\Gamma(-t-s-u-\frac{1}{2})}{\Gamma(-u-t+\frac{1}{4})\Gamma(-t-s+\frac{1}{2})\Gamma(-s-u+\frac{1}{4})}
\end{aligned}$$

By talking about the correct momentum expansion we will actually understand that how to gain all infinite scalar and gauge poles for different  $p, n$  values and how to interpret them in field theory and look for new couplings in the world volume of brane anti brane systems. We also explain why we do not have any tachyon pole in  $\langle V_C V_\phi V_T V_T \rangle$ .

### 3 Momentum expansion for brane-anti brane systems

To be able to look for all couplings in string theory, we need to expand the complete form of the S-matrix elements to find all singular terms (poles) and contact interactions. However due to presence of tachyons here the expansion is no longer the low energy expansion. Therefore we are not allowed to use the limit of  $\alpha' \rightarrow 0$  of the above string amplitude. Turning into Mandelstam variables and using the momentum conservation along the world volume of brane,  $2k_1^a + 2k_2^a + 2k_3^a + p^a + (p \cdot D)^a = 0$ , we obtain a very useful constraint as follows

$$s + t + u = -p_a p^a - \frac{1}{2}. \tag{10}$$

In [17] we discussed in detail that the momentum expansion for various amplitudes should be found either by  $(k_i + k_j)^2 \rightarrow 0$  or  $k_i \cdot k_j \rightarrow 0$ . The first case takes place when we



do have a massless pole and for the other cases we should use  $k_i \cdot k_j \rightarrow 0$  expansion. Due to non-zero two tachyon one gauge coupling, we realize that our amplitude  $C\phi TT$  has to have a massless pole in  $-(k_3 + k_2)^2 = u$  channel. It should only have infinite scalar poles in  $t' + s' + u$  channel ( $t' = t + \frac{1}{4}, s' = s + \frac{1}{4}$ ) and it will become clear later on.

The extremely important point for brane -anti brane systems is that the quantity  $p^a p_a$  should tend to zero while in non-BPS systems due to kinematic constraints (which Mandelstam variables justify) our amplitude like  $C\phi\phi T$  [17] makes sense just by sending  $p^a p_a$  to  $\frac{1}{4}$ .

Keeping in mind above arguments, we understand that the correct momentum expansion in brane anti brane system is indeed

$$(k_3 + k_2)^2 \rightarrow 0, \quad k_1 \cdot k_3 \rightarrow 0, \quad k_2 \cdot k_1 \rightarrow 0.$$

Also using the on-shell relations  $k_1^2 = 0$  and  $k_2^2 = k_3^2 = \frac{1}{4}$  the above momentum expansion can be interpreted in terms of Mandelstam variables as

$$u \rightarrow 0, \quad s \rightarrow \frac{-1}{4}, \quad t \rightarrow \frac{-1}{4} \quad (11)$$

Therefore  $C\phi TT$  should be performed just by setting  $p_a p^a \rightarrow 0$  in brane-anti brane systems.

Applying (11) into the general form of the amplitude, we conclude the poles of the Gamma functions. Hence our amplitude for  $p = n$  case, has infinite u-channel gauge poles meanwhile it does have infinite scalar poles for  $p + 2 = n$  case. Note that since the two tachyons, one scalar field coupling is vanished, we no longer have tachyon pole, rather than in  $CATT$  amplitude for  $p = n$  case we had infinite tachyon poles.

Now we would like to expand our amplitude around (11) to find new couplings out and also to gain the correct two tachyon two scalar couplings of brane anti brane systems to all orders in  $\alpha'$ . We also do want to confirm all order corrections to the Wess-Zumino effective actions of BPS branes which have recently been constructed in [33, 34]. By deriving the closed form of the expansions, we search about several new couplings in field theory and set their coefficients precisely and eventually find all their infinite higher derivative corrections thereof.

### 3.1 Infinite u-channel gauge poles and contact interactions for $p = n$ case

The amplitude was anti symmetrized with respect to interchanging two external tachyons therefore both four point amplitudes of  $C\phi T_1 T_1$  and  $C\phi T_2 T_2$  make no sense in this case. By performing the trace, the ultimate form of the amplitude of  $C\phi T_1 T_2$  becomes

$$\mathcal{A}^{C\phi T_1 T_2} = -8\xi_{1i}k_{3b}k_{2a}2^{-3/2}\frac{16}{(p)!}\left(\epsilon^{a_0\cdots a_{p-2}ba}H_{a_0\cdots a_{p-2}}^i\right)L_1 \quad (12)$$

Let us include the expansion of  $L_1$  around (11) at leading orders

$$L_1 = \pi^{3/2}\left(\frac{-1}{u} + 4\ln(2) + \left(\frac{\pi^2}{6} - 8\ln(2)^2\right)u - \frac{\pi^2}{6}\frac{(s' + t')^2}{u} + \cdots\right) \quad (13)$$

such that  $s' = s + \frac{1}{4}$ ,  $t' = t + \frac{1}{4}$ .

It is clear from (13) that the first term is pole, thus we have to produce this simple pole in field theory as well although as we will see later this part of the S-matrix involves infinite gauge poles, however for the moment let us proceed order by order. In order to produce that gauge pole, we should have taken the following Feynman rule :

$$\mathcal{A} = V_a(C_{p-1}, \phi, A)G_{ab}(A)V_b(A, T_1, T_2) \quad (14)$$

with

$$\begin{aligned} G_{ab}(A) &= \frac{i\delta_{ab}}{(2\pi\alpha')^2 T_p k^2} \\ V_b(A, T_1, T_2) &= T_p(2\pi\alpha')(k_{2b} - k_{3b}) \end{aligned} \quad (15)$$

Note that in the propagator  $k^2$  is indeed  $-\frac{\alpha'}{2}(k_2 + k_3)^2 = u$ . To make field theory obvious, we just point out that the so called  $\text{Tr}(\frac{-1}{4}F_{ab}F^{ba})$ (gauge field's kinetic term) is incharge of propagator.

$V_b(A, T_1, T_2)$  has been found from  $\text{Tr}(2\pi\alpha'D_a T D^a T)$  (tachyon's kinetic term), by applying direct field theory techniques.

In order to obtain that pole we need to actually have the coupling of  $V_a(C_{p-1}, \phi, A)$  as follows:

$$\mu_p \lambda(2\pi\alpha') \int_{\sum_{(p+1)}} \text{Tr}\left(\partial_i C_{p-1} \wedge F(\phi_1 + \phi_2)^i\right) \quad (16)$$

$\lambda = 2\pi\alpha'$  and we used the fact that amplitude is antisymmetric. The scalar field was found from Taylor expansion. Note that this coupling without  $\phi_2^i$  has been firstly pointed out in [33] and it was obtained by carrying out direct computation of  $C\phi AA$  amplitude in the world volume of BPS branes. Having set (16), we get to

$$V_a(C_{p-1}, \phi, A) = \mu_p(2\pi\alpha')^2 \frac{1}{(p)!} \epsilon_{a_0 \dots a_{p-2}} H^{ia_0 \dots a_{p-2}} k_a \xi_i$$

with  $k$  becomes the off-shell gauge field's momentum and it is  $k_a = -(k_2 + k_3)_a$ . It does not need so much work to indeed show that by normalizing the amplitude with a coefficient of  $\frac{i\mu_p}{4\sqrt{2\pi}}$  and using (14) the first gauge pole in (13) will precisely be resulted.

Now we come to interesting point which is discovering new couplings. As it is clear from the expansion, the second term in (13) is contact term so in order to produce this term the following coupling should have been considered

$$\frac{i}{2} \mu_p \beta^2 (2\pi\alpha')^3 \text{Tr} \left( \partial_i C_{p-1} \wedge DT \wedge DT^* (\phi^1 + \phi^2)^i \right) \quad (17)$$

Thus by extracting this new Wess-Zumino coupling as follows

$$A_c = \mu_p \beta^2 (2\pi\alpha')^3 \frac{i}{2p!} \epsilon_{a_0 \dots a_p} H^{ia_0 \dots a_{p-2}} k^{3a_{p-1}} k^{2a_p} \xi^i \quad (18)$$

we actually could exactly produce the second term of the expansion. Notice that  $\beta$  is a normalization constant in Wess-Zumino terms which has been fixed in [19].

Again the third term of the expansion is contact interaction. A very important question comes out is that how we can talk about the other terms appeared in (13). The simple expectation is that the other terms must be related to higher derivative corrections of the new couplings so having applied this remarkable argument, we are led to the following coupling

$$\frac{i}{2} \mu_p (2\pi\alpha') (\alpha')^2 \left( \frac{\pi^2}{6} - 8 \ln 2^2 \right) \text{Tr} \left( \partial_i C_{p-1} \wedge D^a D_a (DT \wedge DT^*) (\phi^1 + \phi^2)^i \right) \quad (19)$$

Having used the higher derivative correction to the coupling of

$$\text{Tr} \left( \partial_i C_{p-1} \wedge DT \wedge DT^* (\phi^1 + \phi^2)^i \right)$$

as appeared in (19), we could produce the third term of the expansion in (13) in a correct manner, so not only could we find new coupling like (17) but also we could fix its coefficient and also we obtained its extensions in (19) as well.

The other fascinating fact which we must emphasize is that, the expansion (13) dictates us that our S-matrix has namely infinitely many gauge poles. For example the fourth term in the expansion of (13) is again simple pole. All the infinite gauge poles are going to produce by the same Feynman rule (14) but two subtleties are in order. First of all the whole infinite gauge poles will show us that the term of  $\text{Tr}(2\pi\alpha'D_aTD^aT)$  or in the other words, tachyon's kinetic term does not receive any higher derivative correction. This is related to the fact that this kinetic term or  $\text{Tr}(2\pi\alpha'D_aTD^aT)$  has been fixed in tachyon effective action. Second of all, the natural point comes out is that, the only approach to obtain all infinite gauge poles is that, the vertex of  $V_a(C_{p-1}, A, \phi^i)$  must get improved to indeed have all poles in field theory analysis as well.

For example the second pole for this amplitude is produced by embedding the following vertex in the Feynman amplitude (14)

$$V_a(C_{p-1}, \phi, A) = \frac{(\alpha'\pi)^2}{6} \mu_p (2\pi\alpha')^2 \frac{1}{(p)!} \epsilon_{a_0 \dots a_{p-2}} H^{ia_0 \dots a_{p-2}} k_a \xi_i (k_1 \cdot p)^2$$

Now in order to produce all infinite gauge poles, the complete form of the expansion of  $L_1$  is needed. After applying some identities, the closed form of the expansion of  $L_1$  around (11) to all orders in  $\alpha'$  will be explored as follows

$$L_1 = \pi^{3/2} \left( -\frac{1}{u} \sum_{n=-1}^{\infty} b_n (s' + t')^{n+1} + \sum_{p,n,m=0}^{\infty} f_{p,n,m} u^p (s't')^n (s' + t')^m \right) \quad (20)$$

with  $f_{p,0,0} = a_p$  and the following coefficients must be considered

$$\begin{aligned} b_{-1} &= 1, b_0 = 0, b_1 = \frac{\pi^2}{6}, b_2 = 2\zeta(3), a_0 = 4\ln 2, \\ a_1 &= \frac{\pi^2}{6} - 8\ln(2)^2, a_2 = \frac{2}{3}(-\pi^2 \ln 2 + 3\zeta(3) + 16\ln(2)^3), \\ f_{0,0,2} &= \frac{2}{3}\pi^2 \ln(2), f_{0,1,0} = -14\zeta(3), f_{0,0,3} = 8\zeta(3) \ln(2), \\ f_{1,1,0} &= 56\zeta(3) \ln(2) - 1/2, f_{1,0,2} = \frac{1}{36}(\pi^4 - 48\pi^2 \ln(2)^2), f_{0,1,1} = -1/2 \end{aligned} \quad (21)$$

Note that some of these coefficients are completely different from those appeared in the world volume of non-BPS branes [17]. However it is quite interesting that  $b_n$  coefficients here are precisely the same  $b_n$ 's that were appeared in the momentum expansion of BPS branes like  $b_n$  coefficients in the S-matrix elements of  $C AAA$  in [5].

By imposing the infinite higher derivative corrections as

$$\mu_p \lambda (2\pi\alpha') \int_{\Sigma_{(p+1)}} \partial_i C_{p-1} \wedge \sum_{n=-1}^{\infty} b_n (\alpha')^{n+1} \text{Tr} \left( D_{a_1} \cdots D_{a_{n+1}} F D^{a_1} \cdots D^{a_{n+1}} (\phi_1 + \phi_2)^i \right) \quad (22)$$

and deriving the vertex of  $V_a(C_{p-1}, \phi, A)$  as

$$V_a(C_{p-1}, \phi, A) = \mu_p (2\pi\alpha')^2 \frac{1}{(p)!} \epsilon_{a_0 \cdots a_{p-2}} H^{ia_0 \cdots a_{p-2}} (k_2 + k_3)^a \xi_i \sum_{n=-1}^{\infty} b_n (\alpha' k_1 \cdot k)^{n+1}$$

and replacing it in (14) we end up with

$$\mathcal{A} = \mu_p (2\pi\alpha') \frac{2i}{(p)! u} \epsilon_{a_0 \cdots a_{p-2} ab} H^{ia_0 \cdots a_{p-2}} k_2^b k_3^a \xi_i \sum_{n=-1}^{\infty} b_n \left( \frac{\alpha'}{2} \right)^{n+1} (s' + t')^{n+1} \quad (23)$$

By replacing the first term of (20) in (12) and comparing (23) with (12) we actually clarified that the infinite string theory 'gauge poles are precisely produced. The other remarkable fact which should be emphasized is that, concerning the above amplitude (12) with the infinite gauge poles of the field theory amplitude, that is, (23) we have no longer any residual contact interactions for this part of the amplitude which does satisfy  $p = n$  case.

Let us end this part of the amplitude by searching about all contact terms of  $C\phi TT$  amplitude as below

$$- \frac{i}{2} \mu_p \pi \xi_{1i} k_{3b} k_{2a} \frac{16}{(p)!} \left( \epsilon^{a_0 \cdots a_{p-2} ba} H_{a_0 \cdots a_{p-2}}^i \right) \sum_{p,n,m=0}^{\infty} f_{p,n,m} u^p (s' t')^n (s' + t')^m \quad (24)$$

Working out in detail we can show that the closed form of all infinite contact terms of string theory amplitude for  $p = n$  case, will be concluded in the field theory by taking into account the following couplings to all orders in  $\alpha'$  :

$$2i\alpha' (\pi\alpha') \mu_p \sum_{p,n,m=0}^{\infty} f_{p,n,m} \left( \frac{\alpha'}{2} \right)^p (\alpha')^{2n+m} \partial_i C_{p-1} \wedge (D^a D_a)^p D_{b_1} \cdots D_{b_m} (D_{a_1} \cdots D_{a_n} D T \wedge D_{a_{n+1}} \cdots D_{a_{2n}} D T^*) \partial^{a_1} \cdots \partial^{a_{2n}} \partial^{b_1} \cdots \partial^{b_m} (\phi_1 + \phi_2)^i \quad (25)$$

Note that in the above coupling we could consider covariant derivative of scalar, however it turns out that the commutator in the definition of covariant derivative of scalar should not be considered here as we are looking for  $C\phi TT$  coupling. A good question is to see whether or not covariant derivative of scalar keeps fixed in the above coupling. To answer this question one has to carry out a six point function, basically checking  $C\phi ATT$  amplitude will be worth working out, nevertheless we can not come over to this remark by our computations of this paper.

### 3.2 Infinite $(u + s' + t')$ -channel scalar poles and contact interactions for $p + 2 = n$

Having performed the trace, we can take all non-zero terms of the string amplitude for this certain case as

$$\mathcal{A}^{\phi T_1 T_1 C} = \pm \frac{8i\mu_p}{\sqrt{\pi}(p+1)!} L_2 \epsilon^{a_0 \dots a_p} H_{a_0 \dots a_p}^i \xi_i \quad (26)$$

As it follows from the amplitude and unlike the first part of the amplitude, in this section our S-matrix is symmetric, that is, by interchanging two tachyons the amplitude remains unchanged. Therefore  $C\phi T_1 T_2$  amplitude does not contribute to  $p+2 = n$  case. As a matter of fact our calculations make sense either for  $C\phi T_1 T_1$  or  $C\phi T_2 T_2$  amplitudes. Note that due to kinematic reasons, we can not talk about associated ward identities either.

The expansion of  $L_2$  at leading order around (11) is

$$\begin{aligned} L_2 = & \frac{\sqrt{\pi}}{2} \left( \frac{-1}{(t' + s' + u)} + 4 \ln(2) + \left( \frac{\pi^2}{6} - 8 \ln(2)^2 \right) (s' + t' + u) \right. \\ & \left. - \frac{\pi^2}{3} \frac{t' s'}{(t' + s' + u)} + \dots \right) \end{aligned} \quad (27)$$

The first scalar pole in  $t' + s' + u$ -channel should be produced by taking the following amplitude

$$\begin{aligned} \mathcal{A} = & V_i(C_{p+1}, \phi^{(1)}) G_{ij}(\phi) V_j(\phi^{(1)}, T_1, T_1, \phi^{(1)}) \\ & + V_i(C_{p+1}, \phi^{(2)}) G_{ij}(\phi) V_j(\phi^{(2)}, T_1, T_1, \phi^{(1)}) \end{aligned} \quad (28)$$

It is important to highlight the fact that in order to have consistent result  $\phi$  in the propagator must be  $\phi^{(1)}$  and  $\phi^{(2)}$ . The needed vertices can be read off as

$$\begin{aligned}
G_{ij}(\phi) &= \frac{i\delta_{ij}\delta_{\alpha\beta}}{(2\pi\alpha')^2 T_p (u+t'+s')} \\
V_i(C_{p+1}, \phi^{(1)}) &= i\mu_p(2\pi\alpha') \frac{1}{(p+1)!} \epsilon^{a_0 \dots a_p} H_{ia_0 \dots a_p} \text{Tr}(\lambda_\alpha) \\
V_i(C_{p+1}, \phi^{(2)}) &= -i\mu_p(2\pi\alpha') \frac{1}{(p+1)!} \epsilon^{a_0 \dots a_p} H_{ia_0 \dots a_p} \text{Tr}(\lambda_\alpha) \\
V_j(\phi^{(1)}, T_1, T_1, \phi^{(1)}) &= -2iT_p(2\pi\alpha') \xi_j \text{Tr}(\lambda_1 \lambda_2 \lambda_3 \lambda_\beta) \\
V_j(\phi^{(2)}, T_1, T_1, \phi^{(1)}) &= 2iT_p(2\pi\alpha') \text{Tr}(\lambda_1 \lambda_2 \lambda_3 \lambda_\beta) \xi_j
\end{aligned} \tag{29}$$

Now by applying the above vertices into (28) we reach to

$$\mathcal{A} = \frac{4i\mu_p}{(p+1)!(u+s'+t')} \epsilon^{a_0 \dots a_p} H_{ia_0 \dots a_p} \xi^i \tag{30}$$

By substituting (27) into (28) and comparing the result with (30) we get the fact that the first scalar pole in  $u+t'+s'$ -channel has been precisely obtained.

Let us consider the first contact interaction in (27) as follows

$$\mathcal{A}_c = i\mu_p \ln(2) \frac{16}{(p+1)!} \epsilon^{a_0 \dots a_p} H_{ia_0 \dots a_p} \xi^i \tag{31}$$

It is remarkable that in order to produce (31), we should explore another new coupling and indeed fix its coefficient, which is the only way to do so,

$$\frac{\mu_p}{(p+1)!} (2\pi\alpha')^2 \beta^2 \partial_i C_{a_0 \dots a_p} (\phi^{(1)} - \phi^{(2)})^i |T|^2 \epsilon^{a_0 \dots a_p} \tag{32}$$

In order to find out the third term in the expansion of (27), we believe that it will be produced just by applying higher derivative on the above coupling as

$$-(\alpha')^2 \frac{\mu_p}{(p+1)!} \left( \frac{\pi^2}{6} - 8 \ln(2)^2 \right) \partial_i C_{a_0 \dots a_p} D^a D_a \left[ (\phi^{(1)} - \phi^{(2)})^i |T|^2 \right] \epsilon^{a_0 \dots a_p} \tag{33}$$

Another way of writing this higher extension is as follows :

$$-(\alpha')^2 \frac{\mu_p}{(p+1)!} \left( \frac{\pi^2}{6} - 8 \ln(2)^2 \right) \epsilon^{a_0 \dots a_p} H_{ia_0 \dots a_p} \partial^a \partial_a \left[ (\phi^{(1)} - \phi^{(2)})^i T T^* \right] \tag{34}$$

It is really important to note that, we have to consider this coupling and in particular the difference between the first scalar (which is on the brane) and the second scalar (which is on the anti brane) has to appear, to be able to produce the third term of the expansion in (27).

Likewise the last section , we are going to find out the closed form of the expansion of  $L_2$  around (11) as

$$L_2 = \frac{\sqrt{\pi}}{2} \left( \frac{-1}{(t' + s' + u)} + \sum_{n=0}^{\infty} a_n (s' + t' + u)^n + \frac{\sum_{n,m=0}^{\infty} l_{n,m} (s' + t')^n (t' s')^{m+1}}{(t' + s' + u)} + \sum_{p,n,m=0}^{\infty} e_{p,n,m} (s' + t' + u)^p (s' + t')^n (t' s')^{m+1} \right) \quad (35)$$

$l_{n,m}$  and  $e_{p,n,m}$  are

$$\begin{aligned} l_{0,0} &= -\pi^2/3, & l_{1,0} &= 8\zeta(3) \\ l_{2,0} &= -7\pi^4/45, & l_{0,1} &= \pi^4/45, & l_{3,0} &= 32\zeta(5), & l_{1,1} &= -32\zeta(5) + 8\zeta(3)\pi^2/3 \\ e_{0,0,0} &= \frac{2}{3} \left( 2\pi^2 \ln(2) - 21\zeta(3) \right), & e_{1,0,0} &= \frac{1}{9} \left( 4\pi^4 - 504\zeta(3) \ln(2) + 24\pi^2 \ln(2)^2 \right) \end{aligned} \quad (36)$$

It is highly important to trust this special expansion in order to distinguish the last contact terms of (35) from the second terms of expansion in (35). Indeed the last terms in (35) do have different structure so we come to the fact that the last term of the expansion must be produced by making use of the different couplings in field theory.

Using the arguments we have mentioned earlier, we can write down a higher derivative coupling to produce the second term in (35). In the other words it is produced by taking this higher extension of the coupling

$$-(\alpha')^2 \frac{\mu_p}{(p+1)!} \sum_{n=0}^{\infty} a_n \left( \frac{\alpha'}{2} \right)^n \epsilon^{a_0 \dots a_p} H_{ia_0 \dots a_p} (\partial^a \partial_a)^n \left[ (\phi^{(1)} - \phi^{(2)})^i T T^* \right] \quad (37)$$

Remember that we found these couplings with using the S-matrix of string theory, thus we believe that here all on-shell ambiguities for these new couplings are removed.

As it is clear from the closed form of the expansion of  $L_2$  in (35), it does involve the infinite scalar poles in  $t' + s' + u$ -channel for  $p+2 = n$  case. Let us write down in a precise way all the infinite scalar poles in string theory once more:



$$\mathcal{A}^{C\phi T_2 T_2} = \frac{4i\mu_p}{(p+1)!} \epsilon^{a_0 \dots a_p} H_{ia_0 \dots a_p} \left( \xi^i s' t' \right) \frac{\sum_{n,m=0}^{\infty} l_{n,m} (s' + t')^n (t' s')^m}{(t' + s' + u)} \quad (38)$$

In this subsection, we want to check that the recent all order two scalar two tachyon couplings of non-BPS branes (equation (36) [17]) will not produce infinite massless scalar poles of brane anti brane 's string theory amplitude of  $C\phi T_2 T_2$  which exist in  $(s' + t' + u)$ -channel. Thus we conclude that, one has to discover the new all order higher derivative corrections of two tachyon, two scalar couplings of brane anti brane systems. Finally in order to show that we have found the correct corrections to two tachyon two scalar couplings to all orders in brane anti brane systems we make a consistent check. In fact by making use of these new higher derivative corrections we exactly produce all the infinite scalar poles in  $u + t' + s'$  channel. Although we do not explain all details for corrections, we just make a comment that the appearance of  $\sigma_3$  Chan-Paton factor for scalar field in (-1)-picture plays a crucial role to actually obtain these corrections.

The Lagrangian for two scalar, two tachyon couplings for non-BPS brane was defined as

$$\begin{aligned} \mathcal{L}(\phi, \phi, T, T) = & -2T_p(\pi\alpha')^3 \text{STr} \left( m^2 T^2 (D_a \phi^i D^a \phi_i) + \frac{\alpha'}{2} D^\alpha T D_\alpha T D_a \phi^i D^a \phi_i \right. \\ & \left. - \alpha' D^b T D^a T D_a \phi^i D_b \phi_i \right) \end{aligned} \quad (39)$$

Having extracted symmetrized traces, the higher derivative corrections of two scalars, two tachyons for non-BPS branes to all orders in  $\alpha'$  have been found in [17] as

$$\mathcal{L} = -2T_p(\pi\alpha')(\alpha')^{2+n+m} \sum_{n,m=0}^{\infty} (\mathcal{L}_1^{nm} + \mathcal{L}_2^{nm} + \mathcal{L}_3^{nm} + \mathcal{L}_4^{nm}), \quad (40)$$

where

$$\begin{aligned} \mathcal{L}_1^{nm} &= m^2 \text{Tr} \left( a_{n,m} [\mathcal{D}_{nm}(T^2 D_a \phi^i D^a \phi_i) + \mathcal{D}_{nm}(D_a \phi^i D^a \phi_i T^2)] \right. \\ &\quad \left. + b_{n,m} [\mathcal{D}'_{nm}(T D_a \phi^i T D^a \phi_i) + \mathcal{D}'_{nm}(D_a \phi^i T D^a \phi_i T)] + h.c. \right), \\ \mathcal{L}_2^{nm} &= \text{Tr} \left( a_{n,m} [\mathcal{D}_{nm}(D^\alpha T D_\alpha T D_a \phi^i D^a \phi_i) + \mathcal{D}_{nm}(D_a \phi^i D^a \phi_i D^\alpha T D_\alpha T)] \right. \\ &\quad \left. + b_{n,m} [\mathcal{D}'_{nm}(D^\alpha T D_a \phi^i D_\alpha T D^a \phi_i) + \mathcal{D}'_{nm}(D_a \phi^i D_\alpha T D^a \phi_i D^\alpha T)] + h.c. \right), \\ \mathcal{L}_3^{nm} &= -\text{Tr} \left( a_{n,m} [\mathcal{D}_{nm}(D^\beta T D_\mu T D^\mu \phi^i D_\beta \phi_i) + \mathcal{D}_{nm}(D^\mu \phi^i D_\beta \phi_i D^\beta T D_\mu T)] \right. \end{aligned}$$

$$\begin{aligned}
& + b_{n,m} [\mathcal{D}'_{nm} (D^\beta T D^\mu \phi^i D_\mu T D_\beta \phi_i) + \mathcal{D}'_{nm} (D^\mu \phi^i D_\mu T D_\beta \phi_i D^\beta T)] + h.c. \Big), \\
\mathcal{L}_4^{nm} = & -\text{Tr} \left( a_{n,m} [\mathcal{D}_{nm} (D^\beta T D^\mu T D_\beta \phi^i D_\mu \phi_i) + \mathcal{D}_{nm} (D^\beta \phi^i D^\mu \phi_i D_\beta T D_\mu T)] \right. \\
& \left. + b_{n,m} [\mathcal{D}'_{nm} (D^\beta T D_\beta \phi^i D^\mu T D_\mu \phi_i) + \mathcal{D}'_{nm} (D_\beta \phi^i D_\mu T D^\mu \phi_i D^\beta T)] + h.c. \right) \quad (41)
\end{aligned}$$

Note that the definitions of  $\mathcal{D}_{nm}(EFGH)$  and  $\mathcal{D}'_{nm}(EFGH)$  were given in [17]. Let us show in a clear way that these corrections do not work for brane anti brane systems, namely we want to emphasize that by using them we can not produce all the infinite scalar poles in  $u + t' + s'$ -channel so it definitely means that they are not correct corrections for brane anti brane systems.

The Feynman rule for this particular case is

$$\mathcal{A} = V_\alpha^i(C_{p+1}, \phi) G_{\alpha\beta}^{ij}(\phi) V_\beta^j(\phi, \phi_1, T_2, T_2), \quad (42)$$

with

$$\begin{aligned}
G_{\alpha\beta}^{ij}(\phi) &= \frac{-i\delta_{\alpha\beta}\delta^{ij}}{T_p(2\pi\alpha')^2 k^2} = \frac{-i\delta_{\alpha\beta}\delta^{ij}}{T_p(2\pi\alpha')^2 (t' + s' + u)}, \\
V_\alpha^i(C_{p+1}, \phi) &= i(2\pi\alpha')\mu_p \frac{1}{(p+1)!} \epsilon^{a_0 \dots a_p} H_{a_0 \dots a_p}^i \text{Tr}(\lambda_\alpha). \quad (43)
\end{aligned}$$

$\lambda_\alpha$  is an Abelian matrix. Having considered off-shell 's scalar field which is Abelian and taking two permutations as

$$\text{Tr}(\lambda_2 \lambda_3 \lambda_1 \lambda_\beta), \text{Tr}(\lambda_2 \lambda_3 \lambda_\beta \lambda_1)$$

,  $V_\beta^j(\phi, \phi_1, T_2, T_2)$  should be derived from the higher derivative couplings in (41) as

$$\begin{aligned}
V_\beta^j(\phi, \phi_1, T_2, T_2) = & \xi_1^j I_9 (-2iT_p\pi)(\alpha')^{n+m+3} (a_{n,m} + b_{n,m}) \Big( (k_2 \cdot k_1)^n (k \cdot k_2)^m + (k_2 \cdot k_1)^n (k_3 \cdot k_1)^m \\
& + (k_2 \cdot k)^n (k_1 \cdot k_2)^m + (k \cdot k_2)^n (k \cdot k_3)^m + (k_3 \cdot k)^n (k_2 \cdot k)^m + (k_3 \cdot k)^n (k_3 \cdot k_1)^m \\
& + (k_1 \cdot k_3)^n (k_2 \cdot k_1)^m + (k_3 \cdot k_1)^n (k_3 \cdot k)^m \Big), \quad (44)
\end{aligned}$$

like previous notations  $k$  becomes off-shell scalar field's momentum, and

$$I_9 = \text{Tr}(\lambda_1 \lambda_2 \lambda_3 \lambda_\beta) \frac{1}{2} (s')(t') \quad (45)$$

$b_{n,m}$  is symmetric, see [5]. Although the coefficients have been mentioned in [17], listing some of the coefficients like  $a_{n,m}$  and  $b_{n,m}$  is important to address :

$$\begin{aligned}
a_{0,0} &= -\frac{\pi^2}{6}, \quad b_{0,0} = -\frac{\pi^2}{12}, \quad a_{1,0} = 2\zeta(3), \quad a_{0,1} = 0, \quad b_{0,1} = -\zeta(3), \quad a_{1,1} = a_{0,2} = -7\pi^4/90, \\
a_{2,2} &= (-83\pi^6 - 7560\zeta(3)^2)/945, \quad b_{2,2} = -(23\pi^6 - 15120\zeta(3)^2)/1890, \quad a_{1,3} = -62\pi^6/945, \\
a_{2,0} &= -4\pi^4/90, \quad b_{1,1} = -\pi^4/180, \quad b_{0,2} = -\pi^4/45, \quad a_{0,4} = -31\pi^6/945, \quad a_{4,0} = -16\pi^6/945, \\
a_{1,2} &= a_{2,1} = 8\zeta(5) + 4\pi^2\zeta(3)/3, \quad a_{0,3} = 0, \quad a_{3,0} = 8\zeta(5), \quad b_{1,3} = -(12\pi^6 - 7560\zeta(3)^2)/1890, \\
a_{3,1} &= (-52\pi^6 - 7560\zeta(3)^2)/945, \quad b_{0,3} = -4\zeta(5), \quad b_{1,2} = -8\zeta(5) + 2\pi^2\zeta(3)/3, \\
b_{0,4} &= -16\pi^6/1890.
\end{aligned} \tag{46}$$

One needs to use the following relations as well

$$k_3 \cdot k = k_2 \cdot k_1 - k^2, \quad k_2 \cdot k = k_1 \cdot k_3 - k^2$$

By ignoring some of the contact interactions (we go through them in the next section), we get all poles in field theory as

$$8i\mu_p \frac{\epsilon^{a_0 \dots a_p} \xi_i H_{a_0 \dots a_p}^i}{(p+1)!(s' + t' + u)} \text{Tr}(\lambda_1 \lambda_2 \lambda_3) \sum_{n,m=0}^{\infty} (a_{n,m} + b_{n,m}) [s'^m t'^n + s'^n t'^m] s' t' \tag{47}$$

On the other hand all the infinite scalar poles of the amplitude in string theory are given as

$$\mathcal{A}^{\phi_1 T_2 T_2 C} = \pm \frac{4i\mu_p}{(p+1)!} \epsilon^{a_0 \dots a_p} H_{a_0 \dots a_p}^i \frac{\sum_{n,m=0}^{\infty} l_{n,m} (s' + t')^n (t' s')^{m+1}}{(t' + s' + u)} \xi_i \tag{48}$$

Now we show that we can not use the corrections of non-BPS branes for brane anti brane systems. We are going to compare both string and field theory amplitude at zero and first order of  $\alpha'$  such that at zero order in field theory we get

$$16s't'(a_{0,0} + b_{0,0}) = -4\pi^2 s't'$$

while in string theory we get

$$4l_{0,0} s't' = \frac{-4\pi^2}{3} s't'$$

clearly it shows that we can not make those corrections to brane anti brane. Let us also see what happens at first order of  $\alpha'$  in string side.

At  $\alpha'$  order, the field theory amplitude has

$$8s't'(s' + t')(a_{1,0} + a_{0,1} + b_{0,1} + b_{0,1}) = 0$$

while in string theory at first order we get

$$4l_{1,0}s't'(s' + t') = 32\zeta(3)s't'(s' + t')$$

Therefore it becomes obvious we have to find out the correct higher derivative corrections of brane anti brane systems to all orders of  $\alpha'$  in order to be able to produce all infinite massless scalar poles in  $t' + s' + u$ - channel as well. In the next section we construct and check them out.

### 3.3 Higher derivative corrections to two tachyon-two scalar couplings for brane anti brane systems to all orders in $\alpha'$

In this section we are going to propose higher derivative corrections to two tachyons, two scalar field couplings in brane anti brane systems to all orders in  $\alpha'$ . As it is obvious the action for brane anti brane system might be constructed by making use of the projection on the effective actions of two unstable branes. Indeed the projection is  $(-1)^{F_L}$  where  $F_L$  becomes space time 's left handed fermion number. Details for constructing higher derivative corrections to all orders in  $\alpha'$ , for BPS branes in [5, 33, 34], for non-BPS branes in [17, 16] and for brane anti brane systems namely for the couplings between two tachyons and two gauge fields in [19, 39] were given.

In order to avoid so many details we just make a very important point as follows. To derive all the higher derivative corrections it turns out that the internal degree of freedom of the scalar field in (-1)-picture plays the crucial role. It is worth trying to point out once more that brane anti brane couplings to all orders should have been read from non-BPS couplings by taking into account the correct matrices .

By substituting matrices and extracting the related trace, we end up indeed with two scalar field and two tachyon couplings to all orders of  $\alpha'$  for brane anti brane as below:

$$\mathcal{L} = -2T_p(\pi\alpha')(\alpha')^{2+n+m} \sum_{n,m=0}^{\infty} (\mathcal{L}_1^{nm} + \mathcal{L}_2^{nm} + \mathcal{L}_3^{nm} + \mathcal{L}_4^{nm}), \quad (49)$$

where

$$\mathcal{L}_1^{nm} = m^2 \text{Tr} \left( a_{n,m} [\mathcal{D}_{nm}(TT^* D_a \phi^{(1)i} D^a \phi_i^{(1)}) + \mathcal{D}_{nm}(D_a \phi^{(1)i} D^a \phi_i^{(1)} TT^*) + h.c.] \right)$$

$$\begin{aligned}
& -b_{n,m}[\mathcal{D}'_{nm}(TD_a\phi^{(2)i}T^*D^a\phi_i^{(1)}) + \mathcal{D}'_{nm}(D_a\phi^{(1)i}TD^a\phi_i^{(2)}T^*) + h.c.], \\
\mathcal{L}_2^{nm} &= \text{Tr} \left( a_{n,m}[\mathcal{D}_{nm}(D^\alpha TD_\alpha T^*D_a\phi^{(1)i}D^a\phi_i^{(1)}) + \mathcal{D}_{nm}(D_a\phi^{(1)i}D^a\phi_i^{(1)}D^\alpha TD_\alpha T^*) + h.c.] \right. \\
& \quad \left. - b_{n,m}[\mathcal{D}'_{nm}(D^\alpha TD_a\phi^{(2)i}D_\alpha T^*D^a\phi_i^{(1)}) + \mathcal{D}'_{nm}(D_a\phi^{(1)i}D_\alpha TD_a\phi_i^{(2)}D^\alpha T^*) + h.c.] \right), \\
\mathcal{L}_3^{nm} &= -\text{Tr} \left( a_{n,m}[\mathcal{D}_{nm}(D^\beta TD_\mu T^*D^\mu\phi^{(1)i}D_\beta\phi_i^{(1)}) + \mathcal{D}_{nm}(D^\mu\phi^{(1)i}D_\beta\phi_i^{(1)}D^\beta TD_\mu T^*) + h.c.] \right. \\
& \quad \left. - b_{n,m}[\mathcal{D}'_{nm}(D^\beta TD^\mu\phi^{(2)i}D_\mu T^*D_\beta\phi_i^{(1)}) + \mathcal{D}'_{nm}(D^\mu\phi^{(1)i}D_\mu TD_\beta\phi_i^{(2)}D^\beta T^*) + h.c.] \right), \\
\mathcal{L}_4^{nm} &= -\text{Tr} \left( a_{n,m}[\mathcal{D}_{nm}(D^\beta TD^\mu T^*D_\beta\phi^{(1)i}D_\mu\phi_i^{(1)}) + \mathcal{D}_{nm}(D^\beta\phi^{(1)i}D^\mu\phi_i^{(1)}D_\beta TD_\mu T^*) + h.c.] \right. \\
& \quad \left. - b_{n,m}[\mathcal{D}'_{nm}(D^\beta TD_\beta\phi^{(2)i}D^\mu T^*D_\mu\phi_i^{(1)}) + \mathcal{D}'_{nm}(D_\beta\phi^{(1)i}D_\mu TD^\mu\phi_i^{(2)}D^\beta T^*) + h.c.] \right) (50)
\end{aligned}$$

In addition to the above couplings, one has to interchange  $D\phi^{(1)i}$  to  $D\phi^{(2)i}$  just for all the terms involving  $a_{n,m}$  and also interchange  $D\phi^{(1)i} \leftrightarrow D\phi^{(2)i}$  for all  $b_{n,m}$ ' terms and essentially add these terms to above couplings as well.

The other point should be clarified is that here all scalar field's covariant derivatives are indeed partial derivatives. Notice that when fields change very slowly or when  $D^2T, D^2\phi$  are zero then above couplings go back to two scalar, two tachyon couplings of tachyon DBI action. Although here we do not need to actually include gauge fields, however, it is worth trying to point out that

$$D_{a_1} \cdots D_{a_n} T = \partial_{a_1} D_{a_2} \cdots D_{a_n} T - i(A_{a_1}^{(1)} - A_{a_1}^{(2)}) D_{a_2} \cdots D_{a_n} T$$

It is highly recommended that here we discovered the new couplings and in particular all the couplings between  $D\phi^{(1)i}$  and  $D\phi^{(2)i}$  must be appeared.

Now in order to show that we have obtained consistent higher derivative corrections of brane anti brane to all orders in  $\alpha'$ , we would like to use these new couplings to indeed check out all infinite massless scalar poles of our amplitude  $C\phi T_2 T_2$ . This is a very important check to do so.

Therefore consider one RR  $-(p+1)$  and one scalar and two either  $T_1$  or  $T_2$  tachyons for brane anti brane system, the Feynman rule in (42) must be taken as well.

Here as we have mentioned earlier on, at the moment we ignore some contact interactions and just focus on new higher derivative corrections of two scalars two tachyons of brane anti brane, in order to produce all the infinite scalar poles.

Now making use of the new two scalar two tachyon couplings of (50) and taking two possible permutations,  $V_\beta^j(\phi, \phi_1, T_2, T_2)$  might be found as

$$\begin{aligned}
V_\beta^j(\phi_1, \phi_1, T_2, T_2) &= \xi_1^j(-2iT_p\pi)(\alpha')^{n+m+3}(a_{n,m} - b_{n,m}) \Big( (k_2 \cdot k_1)^n (k \cdot k_2)^m + (k_2 \cdot k_1)^n (k_3 \cdot k_1)^m \\
&\quad + (k_2 \cdot k)^n (k_1 \cdot k_2)^m + (k \cdot k_2)^n (k \cdot k_3)^m + (k_3 \cdot k)^n (k_2 \cdot k)^m + (k_3 \cdot k)^n (k_3 \cdot k_1)^m \\
&\quad + (k_1 \cdot k_3)^n (k_2 \cdot k_1)^m + (k_3 \cdot k_1)^n (k_3 \cdot k)^m \Big) \frac{1}{2}(s')(t') \text{Tr}(\lambda_1 \lambda_2 \lambda_3 \lambda_\beta), \quad (51)
\end{aligned}$$

Note that  $\phi$  in the propagator of  $G_{ij}(\phi)$  must be  $\phi^{(1)}, \phi^{(2)}$ . Let us highlight that  $T_2$  is related to the second component of complex scalar tachyon which we pointed out earlier. Considering the following vertices

$$\begin{aligned}
G_{ij}(\phi) &= \frac{i\delta_{ij}\delta_{\alpha\beta}}{(2\pi\alpha')^2 T_p (u + t' + s')} \\
V_i(C_{p+1}, \phi^{(1)}) &= i\mu_p(2\pi\alpha') \frac{1}{(p+1)!} \epsilon^{a_0 \dots a_p} H_{ia_0 \dots a_p} \text{Tr}(\lambda_\alpha) \\
V_i(C_{p+1}, \phi^{(2)}) &= -i\mu_p(2\pi\alpha') \frac{1}{(p+1)!} \epsilon^{a_0 \dots a_p} H_{ia_0 \dots a_p} \text{Tr}(\lambda_\alpha) \\
V_\beta^j(\phi_2, \phi_1, T_2, T_2) &= \xi_1^j(2iT_p\pi)(\alpha')^{n+m+3}(a_{n,m} - b_{n,m}) \Big( (k_2 \cdot k_1)^n (k \cdot k_2)^m + (k_2 \cdot k_1)^n (k_3 \cdot k_1)^m \\
&\quad + (k_2 \cdot k)^n (k_1 \cdot k_2)^m + (k \cdot k_2)^n (k \cdot k_3)^m + (k_3 \cdot k)^n (k_2 \cdot k)^m + (k_3 \cdot k)^n (k_3 \cdot k_1)^m \\
&\quad + (k_1 \cdot k_3)^n (k_2 \cdot k_1)^m + (k_3 \cdot k_1)^n (k_3 \cdot k)^m \Big) \frac{1}{2}(s')(t') \text{Tr}(\lambda_1 \lambda_2 \lambda_3 \lambda_\beta), \quad (52)
\end{aligned}$$

and implementing(51) and (52) into (42) we get all infinite scalar poles in field theory as

$$8i\mu_p \frac{\epsilon^{a_0 \dots a_p} \xi_i H_{a_0 \dots a_p}^i}{(p+1)!(s' + t' + u)} \text{Tr}(\lambda_1 \lambda_2 \lambda_3) \sum_{n,m=0}^{\infty} (a_{n,m} - b_{n,m}) [s'^m t'^n + s'^n t'^m] s' t' \quad (53)$$

Simultaneously all the infinite scalar poles of the string amplitude are

$$\mathcal{A}^{\phi_1 T_1 T_1 C} = \pm \frac{4i\mu_p}{(p+1)!} \epsilon^{a_0 \dots a_p} H_{a_0 \dots a_p}^i \frac{\sum_{n,m=0}^{\infty} l_{n,m} (s' + t')^n (t' s')^{m+1}}{(t' + s' + u)} \xi_i \quad (54)$$

Let us remove common factors and just compare string poles with field theory poles at each order. By setting  $n = m = 0$ , the string amplitude gives rise  $4l_{0,0}s't'$  coefficient. At the same time at zeroth order of  $\alpha'$  the field theory amplitude gives us

$$16s't'(a_{0,0} - b_{0,0}) = -4\frac{\pi^2}{3}s't' = 4l_{0,0}s't'$$

Now we can see that the new two scalar, two tachyon couplings of brane anti brane (50) work out. In  $\alpha'$  order, from string's amplitude we obtain  $4l_{1,0}s't'(s' + t')$  and in particular in field's amplitude we get to

$$8s't'(s' + t')(a_{1,0} + a_{0,1} - b_{0,1} - b_{0,1}) = 32\zeta(3)(s' + t')s't' = 4l_{1,0}s't'(s' + t')$$

For  $(\alpha')^2$  order, string amplitude related to  $4l_{2,0}s't'(s' + t')^2 + 4l_{0,1}(s't')^2$  and field carries

$$\begin{aligned} & 16(s't')^2(a_{1,1} - b_{1,1}) + 8s't'(a_{0,2} + a_{2,0} - b_{0,2} - b_{2,0})[(s')^2 + (t')^2] \\ &= 4s't'(-\frac{7\pi^4}{45}(s' + t')^2 + \frac{\pi^4}{45}s't') = 4(l_{2,0}(s' + t')^2 + l_{0,1}s't')s't' \end{aligned}$$

Finally we would like to check  $\alpha'^3$  order, that is, string amplitude does carry  $4l_{3,0}(s' + t')^3t's' + 4l_{1,1}(s' + t')(s't')^2$  and field amplitude does include

$$\begin{aligned} & 8s't'(a_{3,0} + a_{0,3} - b_{0,3} - b_{3,0})[(s')^3 + (t')^3] + 8s't'(a_{1,2} + a_{2,1} - b_{1,2} - b_{2,1})s't'(s' + t') \\ &= 128\zeta(5)s't'(s'^3 + t'^3) + 8s'^2t'^2(s' + t')(32\zeta(5) + 4\pi^2\zeta(3)/3) \\ &= 4l_{3,0}(s' + t')^3t's' + 4l_{1,1}(s' + t')(s't')^2 \end{aligned}$$

We can easily do check, up to all orders, so we reach to the important point that, we have exactly explored all orders two tachyon, two scalar couplings of brane anti brane systems. Remember that in order to get consistent result, some new couplings like the multiplication of  $D\phi^{(1)i}$  and  $D\phi_i^{(2)}$ , that is,  $(D\phi^{(1)i}.D\phi_i^{(2)})$  has to appear inside these infinite higher derivative corrections, This fact becomes obvious if we concentrate on non zero  $b_{n,m}$  coefficients in (50).

Let us complete our discussions even for contact interactions which have been overlooked in producing infinite poles in field theory analysis. They are given by

$$\begin{aligned} & -i\mu_p(\alpha')^2 \frac{\epsilon^{a_0 \dots a_p} H_{a_0 \dots a_p}^i}{(p+1)!} (-\xi_i(s')(t')) \sum_{n,m=0}^{\infty} (a_{n,m} - b_{n,m}) \\ & \left[ \left( 2 \sum_{\ell=1}^m \binom{m}{\ell} (t'^{m-\ell} s'^{\ell} + s'^{m-\ell} t'^{\ell}) + 2 \sum_{\ell=1}^n \binom{n}{\ell} (t'^{n-\ell} s'^{\ell} + s'^{n-\ell} t'^{\ell}) \right) (\alpha' k^2)^{\ell-1} \right. \\ & \left. + \sum_{\ell=1, j=1}^{n,m} \binom{n}{\ell} \binom{m}{j} (t'^{n-\ell} s'^{m-j} + s'^{n-\ell} t'^{m-j}) (\alpha' k^2)^{\ell+j-1} \right] \end{aligned} \quad (55)$$

These couplings might be written down as

$$\begin{aligned} & i(\alpha')^2 \mu_p \frac{\epsilon^{a_0 \dots a_p} H_{a_0 \dots a_p}^i}{(p+1)!} [-\xi_i s' t'] \\ & \times \sum_{p,n,m=0}^{\infty} e'_{p,n,m} (s' + t' + u)^p (s' + t')^n (t' s')^m \end{aligned} \quad (56)$$

Notice that we can write  $e'_{p,n,m}$  as  $a_{n,m}$  and  $b_{n,m}$ . Some of the contact interactions for  $C\phi T_1 T_1$  may have precise structure like the above couplings so as a fact one has to replace the coefficients  $e_{p,n,m}$  in (35) by  $e_{p,n,m} - e'_{p,n,m}$ .

Concerning some of the on-shell ambiguities, what we can say is that again one has to carry out a five point open super string computation like  $TT\phi\phi A$  in which we can not come over to this long computation in this paper. This problem would remain open question to the future research projects.

Eventually let us end up this section by producing all infinite contact interactions of the  $C\phi T_1 T_1$  amplitude to all orders in  $\alpha'$ . We just need to take into account the last term in (35) such that , all contact interactions for this part of the amplitude can be summarized as

$$4i\mu_p \frac{\epsilon^{a_0 \dots a_p} H_{ia_0 \dots a_p}}{(p+1)!} [\xi^i s' t'] \sum_{p,n,m=0}^{\infty} e_{p,n,m} (s' + t' + u)^p (s' + t')^n ((t')(s'))^m \quad (57)$$

These terms can be reproduced in field theory by taking the following couplings

$$2(\alpha')^2 \mu_p \frac{\epsilon^{a_0 \dots a_p} H_{a_0 \dots a_p}^i}{(p+1)!} \sum_{p,n,m=0}^{\infty} e_{p,n,m} (s' + t' + u)^p (s' + t')^n ((t')(s'))^m \\ \times \left[ \partial_b \partial_c (\phi_1 - \phi_2)_i D^b T_1 D^c T_1 + T_1 \rightarrow T_2 \right]$$

Note that in the above couplings the commutator in the definition of tachyon's covariant derivative should not be considered as we do not have any external gauge field here.

In order to produce all the infinite contact interactions, the following derivative must act on the above coupling as well .

$$\begin{aligned} ((s')(t'))^m H\phi TT &\rightarrow (\alpha')^{2m} H \partial_{a_1} \dots \partial_{a_{2m}} \phi D^{a_1} \dots D^{a_m} T D^{a_{m+1}} \dots D^{a_{2m}} T \\ (s' + t')^n H\phi TT &\rightarrow (\alpha')^n H \partial^{a_1} \dots \partial^{a_n} \phi D_{a_1} \dots D_{a_n} (TT) \\ (s' + t' + u)^p H\phi TT &\rightarrow \left( \frac{\alpha'}{2} \right)^p H (D_a D^a)^p (\phi TT) \end{aligned} \quad (58)$$

One has to pay particular attention to the fact that the above couplings indeed have some on-shell ambiguities.

These ambiguities should be fixed by computing the amplitude of  $CTT\phi\phi$  in the world volume of brane anti brane systems. It is understood by field theory analysis that above couplings definitely will be appeared in the infinite tachyon poles of  $CTT\phi\phi$  amplitude. It would be interesting to carry out this computation in detail.



## 4 Conclusions

In this paper using direct computations, we have obtained the closed form of the amplitude of one RR, two tachyons and one scalar field in the world volume of brane anti brane systems. We discovered that  $V(A, T_1, T_2)$  should not receive any correction and in particular by obtaining infinite higher derivative corrections of one RR, one scalar and one gauge field of brane anti brane we could explore all the infinite gauge poles of the amplitude for  $p = n$  case. The special expansion dictates us that ,by applying the related Feynman rules, leading terms do correspond to the DBI and Wess-Zumino effective actions, however all the other non leading terms in the expansion should be related to their higher derivative corrections.

It is very important to emphasize that we have discovered all the higher derivative corrections to two tachyon, two scalar field couplings to all orders in  $\alpha'$  in the world volume of brane anti brane systems and check them out by producing all the infinite scalar  $u + s' + t'$ -channel poles of our amplitude for  $p + 2 = n$  case.

Infinite gauge poles have provided remarkable information to actually derive all infinite higher derivative corrections of  $\partial_i C_{p-1} \wedge F(\phi_1 + \phi_2)^i$ .

By analysing contact interactions of the amplitude for  $p = n$  case we obtained a new coupling like  $\partial_i C_{p-1} \wedge DT \wedge DT^*(\phi_1 + \phi_2)^i$  and fix its coefficient, we also found all its infinite extensions.

Note that, there is no correction to  $\text{Tr}(\phi^i) H_{ia_0 \dots a_p} \epsilon^{a_0 \dots a_p}$ , therefore all higher scalar poles will provide the complete information for infinite higher derivative corrections to two scalars, two tachyons of brane anti brane systems. Contact interactions for  $p + 2 = n$  give us remarkable clues, not only on new coupling like  $\epsilon^{a_0 \dots a_p} H_{ia_0 \dots a_p} (\phi^{(1)} - \phi^{(2)})^i T T^*$  but also on infinite higher derivative corrections thereof. We also derived a new coupling like

$$2(\alpha')^2 \mu_p \frac{\epsilon^{a_0 \dots a_p} H_{a_0 \dots a_p}^i}{(p+1)!} \sum_{p,n,m=0}^{\infty} e_{p,n,m} (s' + t' + u)^p (s' + t')^n ((t')(s'))^m \\ \times \left[ \partial_b \partial_c (\phi_1 - \phi_2)_i D^b T_1 D^c T_1 + T_1 \rightarrow T_2 \right]$$

it would be interesting to see whether or not commutator in the definition of the covariant derivative of tachyon can be held. To settle this remark, one must carry out  $CTT\phi A$  amplitude in brane anti brane system. It is interesting to perform this amplitude and find out all infinite higher derivative corrections to its effective actions as well. Finally it would be interesting to check  $CTTTT$  amplitude to eventually fix symmetrized trace tachyon effective action in the world volume of brane anti brane systems [40].

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